

# Molecular Weight Distribution and Kinetics of Low-temperature Propene Polymerization with Soluble Vanadium-based Ziegler Catalysts

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A kinetic study has been carried out on the low-temperature polymerization of propene with the soluble catalyst system,  $\text{VCl}_4$  and alkylaluminum ( $\text{AlEt}_2\text{Cl}$ ,  $\text{AlEt}_2\text{Br}$ , or  $\text{AlEt}_3$ ). The rate coefficients of the elementary reactions were evaluated at  $-78^\circ\text{C}$ . The molecular weight distribution function was derived on the basis of the polymerization mechanism. The theoretical distribution curves and experimental distribution curves obtained by use of a gel permeation chromatography agree, supporting the mechanism proposed for the coordination polymerization.

The molecular weight distribution (MWD) of polymers depends on the kinetic scheme of polymerization. Flory<sup>1)</sup> and Bamford *et al.*<sup>2)</sup> derived some distribution functions related to kinetic parameters for vinyl polymerization. Since the advent of gel permeation chromatography,<sup>3)</sup> detailed kinetic investigations on the basis of the MWD data of polymers produced have been carried out for various models of polymerization, such as the radical polymerization of styrene with benzoyl peroxide as initiator<sup>4)</sup> and the radiation-induced polymerization of styrene<sup>5)</sup> and  $\alpha$ -methylstyrene.<sup>6)</sup> Agreement between the theoretical and experimental MWD curves can be regarded as evidence for the proposed kinetic scheme. However, this type of investigation does not seem to have been applied to the coordination polymerization of  $\alpha$ -olefin with Ziegler-type catalysts.

In the present study, carrying out the polymerization of propene with the soluble catalyst mixture of  $\text{VCl}_4$  with alkylaluminum [ $\text{AlEt}_2\text{Cl}$ ,  $\text{AlEt}_2\text{Br}$ , or  $\text{AlEt}_3$  ( $\text{Et}=\text{C}_2\text{H}_5$ )] at  $-78^\circ\text{C}$ , we compare the experimental MWD curves with a theoretical one derived from a proposed kinetic scheme. The catalyst system,  $\text{VCl}_4/\text{AlEt}_2\text{Cl}$ <sup>9)</sup> or  $\text{VCl}_4/\text{AlEt}_2\text{Br}$ ,<sup>7)</sup> at  $-78^\circ\text{C}$  gives the syndiotactic form of polypropylene, whereas  $\text{VCl}_4/\text{AlEt}_3$ <sup>10)</sup> gives the stereoirregular (atactic) form of polypropylene.

The kinetic scheme for polymerization is discussed, values being then determined for the rate coefficients of elementary reactions along the scheme.

## Kinetic Scheme

The mechanism of syndiotactic polymerization of propene with the soluble catalyst system  $\text{VCl}_4/\text{AlEt}_2\text{Cl}$  has been extensively investigated by Natta and co-workers.<sup>8-11)</sup> Their kinetic data<sup>9,10)</sup> on the polymerization and spectroscopic data<sup>11)</sup> of the catalyst system suggest the following mechanistic features concerning the polymerization of propene. The catalytically active vanadium formed by the reaction of  $\text{VCl}_4$  with  $\text{AlEt}_2\text{Cl}$  is only a small fraction (less than 1%) of the total amount of vanadium<sup>9)</sup> and a trivalent state.<sup>11)</sup> The polymerization of propene takes place *via* two successive reactions, propene monomer coordination to the active vanadium and the subsequent insertion of the coordinated monomer into the growing chain attached to the

metal.<sup>10)</sup> The molecular weight of the growing chain is restricted either by the propene monomer coordinated or by the attack of alkylaluminum.<sup>9,10)</sup> The chain transfer with monomer may be caused by a hydrogen transfer from the growing chain to the coordinated monomer with the subsequent formation of a new growing chain and a dead polymer. In the chain transfer with alkylaluminum, the growing chain attached to the vanadium may be replaced by the alkyl group on aluminium. In both cases the number of polymerization centers remains unchanged. For the purpose of calculation, the above reactions are written as follows.

Coordination to monomer



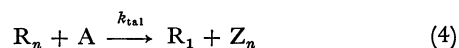
Propagation



Chain transfer with monomer



Chain transfer with alkylaluminium



Here  $\text{C}_n$  and  $\text{R}_n$  represent the growing chain with  $n$  units attached to the active vanadium metal with and without the monomer coordinated, respectively.  $\text{M}$ ,  $\text{A}$ ,  $\text{Y}_n$ , and  $\text{Z}_n$  represent the propene monomer, alkylaluminium, polymer with  $n$  units and polymer molecule with  $n$  units attached to inactive aluminium metal, respectively.

The overall rates of propagation,  $R_p$ , and chain transfer,  $R_t$ , are given by

$$\begin{aligned} R_p &= k_p \sum_1 [\text{C}_n] = k_p K_m \sum_1 [\text{R}_n] [\text{M}] \\ &= k_p \left( \frac{K_m [\text{M}]}{1 + K_m [\text{M}]} \right) \sum_1 ([\text{C}_n] + [\text{R}_n]) \end{aligned} \quad (5)$$

$$R_t = (k_{tm} K_m [\text{M}] + k_{ta1} [\text{A}]) \sum_1 [\text{R}_n] \quad (6)$$

The number average degree of polymerization of the isolated polymers,  $\bar{P}_n$ , at a given time,  $t$ , is given by

$$\bar{P}_n = \frac{\int_0^t R_p dt}{\sum_1 ([\text{C}_n] + [\text{R}_n]) + \int_0^t R_t dt} \quad (7)$$

If we assume the steady-state conditions under which  $R_p$  and  $R_t$  remain constant during the course of polymerization, the reciprocal of  $\bar{P}_n$  can be expressed as

$$\frac{1}{\bar{P}_n} = \left( \frac{1 + K_m[M]}{k_p K_m[M]} \right) \cdot \frac{1}{t} + \frac{R_t}{R_p} \quad (8)$$

Under the conditions that  $t \gg 0$ , Eq. 8 can be approximated as

$$\frac{1}{\bar{P}_n} \simeq \frac{R_t}{R_p} = \frac{k_{tm}}{k_p} + \frac{k_{tai}}{k_p K_m} \cdot \frac{[A]}{[M]} \quad (9)$$

We now derive the MWD function in this polymerization. The formation of the growing chain with  $n$  units is given by

$$\frac{d[R_n + C_n]}{dt} = k_p K_m[M]([R_{n-1}] - [R_n]) - (k_{tm} K_m[M] + k_{tai}[A])[R_n] \quad (10)$$

When the polymerization is stationary, *i.e.*,  $[C_n]$  and  $[R_n]$  remain constant during the course of polymerization, the right-hand side of Eq. 10 is zero. Thus we have

$$[R_n] = \beta[R_{n-1}] = \beta^{n-1}[R_1] \quad (11)$$

$$\text{with } \beta = \frac{k_p K_m[M]}{k_p K_m[M] + k_{tm} K_m[M] + k_{tai}[A]} \quad (12)$$

The rate of formation of the polymer with  $n$  units is given by

$$\frac{d[Y_n + Z_n]}{dt} = (k_{tm} K_m[M] + k_{tai}[A])[R_n] \quad (13)$$

For a low conversion of monomer the concentration of polymer,  $[Y_n + Z_n]$ , may be expressed as a function of  $t$ .

$$[Y_n + Z_n] = (k_{tm} K_m[M] + k_{tai}[A])\beta^{n-1}[R_1]t \quad (14)$$

Thus, we have the mole fraction of polymer with  $n$  units,  $X(n)$

$$X(n) = (1 - \beta)\beta^{n-1} \quad (15)$$

which is the same as the MWD function derived by Flory.<sup>1)</sup>

## Experimental

**Reagents.** Propene (Mistubishi Petrochemical Co. 99.7 % purity, the impurity being propane) was dried by passing through columns of NaOH and P<sub>2</sub>O<sub>5</sub>. Heptane (reagent grade) was dried by refluxing over sodium metal under nitrogen atmosphere after distillation. Alkylaluminiums (Japan Aluminium Alkyl Co.) and VCl<sub>4</sub> (Wako Pure Chemicals) were used without further purification.

**Polymerization Procedure.** A three-necked glass flask with a magnetic stirrer was used as a reactor. Propene was condensed into heptane in the reactor kept at  $-78^\circ\text{C}$  with methanol-Dry Ice. The amount of heptane used was adjusted to be 100 ml as the total volume of solution. Prescribed amounts of alkylaluminium and VCl<sub>4</sub> were charged one after the other. Polymerization was timed from the addition of the VCl<sub>4</sub> component, and quenched at a given time by introducing 100 ml of an ethanol solution of hydrochloric acid cooled at  $-78^\circ\text{C}$ . The polymers obtained were washed several times with 200–300 ml ethanol and dried *in vacuo* at room temperature.

**Gel-permeation Chromatography Analysis.** Molecular weight distributions of polymers were measured by gel permeation chromatography (GPC) (Waters Associates, Model 200) with the use of five polystyrene gel columns (10<sup>7</sup>, 10<sup>6</sup>, 10<sup>5</sup>, 10<sup>4</sup>, and 10<sup>3</sup> Å pore sizes) and *o*-dichlorobenzene as a solvent at 135  $^\circ\text{C}$ . The solvent flow rate was maintained at 1.0 ml/min.

A molecular weight calibration curve was obtained on the basis of the universal calibration,<sup>12,13)</sup> with 10 standard samples of monodisperse polystyrene of molecular weights 2100–2610000. From the GPC data, the number-average and weight-average molecular weights ( $\bar{M}_n$ ,  $\bar{M}_w$ ) were obtained by standard procedures by using the data at 1/2 count (2.5 ml elution volume).

## Results and Discussion

The polymerization results obtained at  $-78^\circ\text{C}$  under various conditions are summarized in Tables 1, 2, and 3 for the VCl<sub>4</sub>/AlEt<sub>2</sub>Cl, VCl<sub>4</sub>/AlEt<sub>2</sub>Br, and VCl<sub>4</sub>/AlEt<sub>3</sub> catalysts, respectively. Polymerization was carried out in the range of a low conversion of propene monomer up to several percents. The concentration of monomer may be regarded as constant during the course of polymerization. Kinetic analysis for the polymerization was made from the data given in the Tables.

**Polymerization Rate.** The time dependence of the yields of polymers produced in the course of polymerizations with different catalyst systems is shown in Fig. 1. The yield-time curves are almost linear with no induction periods. This shows that the formation of the polymerization centers is complete just after the start of polymerization and the number of the centers remains constant during the course of polymerization.

The polymer yields at a given polymerization time were of first-order, as anticipated, with respect to the amount of vanadium tetrachloride at a constant concentration of alkylaluminium. On the other hand, it was found that the relationship between polymerization rate and propene monomer concentration is not of simple first-order kinetics. The polymerization rate,  $R_p$ , increased to a constant value with increase in monomer

TABLE 1. POLYMERIZATION RESULTS OBTAINED AT  $-78^\circ\text{C}$  UNDER DIFFERENT EXPERIMENTAL CONDITIONS WITH VCl<sub>4</sub>/AlEt<sub>2</sub>Cl CATALYST SYSTEM

Sample	AlEt <sub>2</sub> Cl (mol/l)	C <sub>3</sub> H <sub>6</sub> (mol/l)	Polymerization period (h)	Polymer yield (g)	$\bar{M}_n$ ( $\times 10^4$ )	$Q$ ( $\bar{M}_w/\bar{M}_n$ )
A-1	0.05	8.4	0.5	0.05	2.39	1.4
A-2	0.05	8.4	0.75	0.14	2.32	1.5
A-3	0.05	8.4	1.0	0.19	2.99	1.5
A-4	0.05	8.4	2.0	0.49	3.06	1.5
A-5	0.05	8.4	3.0	0.72	3.19	1.5
A-6	0.05	8.4	4.0	1.01	3.73	1.6
A-7	0.05	8.4	5.0	1.39	3.58	1.7
A-8	0.05	8.4	7.0	2.00	4.07	1.7
A-9	0.03	8.4	3.0	0.52	3.28	1.5
A-10	0.10	8.4	3.0	0.99	2.93	1.6
A-11	0.15	8.4	3.0	0.96	3.06	1.7
A-12	0.20	8.4	3.0	0.97	2.68	1.8
A-13	0.25	8.4	3.0	0.94	2.87	1.6
A-14	0.05	1.2	3.0	0.23	1.92	1.9
A-15	0.05	2.4	3.0	0.46	2.27	1.7
A-16	0.05	4.8	3.0	0.66	2.97	1.7
A-17	0.05	11.7	3.0	0.66	—	—

VCl<sub>4</sub> concentration of 0.01 mol/l, polymerization solution of 0.1 l.

TABLE 2. POLYMERIZATION RESULTS OBTAINED  
AT  $-78^{\circ}\text{C}$  WITH  $\text{VCl}_4/\text{AlEt}_2\text{Br}$   
CATALYST SYSTEM

Sample	$\text{AlEt}_2\text{Br}$ (mol/l)	$\text{C}_3\text{H}_6$ (mol/l)	Polymeri- zation period (h)	Poly- mer yield (g)	$\bar{M}_n$ ( $\times 10^3$ )	$Q$ ( $\bar{M}_w/\bar{M}_n$ )
B-1	0.050	8.4	2.0	0.06	3.34	2.3
B-2	0.050	8.4	3.0	0.08	5.17	3.0
B-3	0.050	8.4	5.0	0.10	6.58	2.7
B-4	0.050	8.4	6.5	0.16	5.50	2.6
B-5	0.015	8.4	3.0	0.05	—	—
B-6	0.025	8.4	3.0	0.09	4.24	2.5
B-7	0.075	8.4	3.0	0.04	4.61	1.7
B-8	0.100	8.4	3.0	0.04	4.40	1.6
B-9	0.200	8.4	3.0	0.03	3.34	1.6
B-10	0.025	4.8	3.0	0.06	3.02	2.0
B-11	0.025	12.3	3.0	0.14	4.93	2.3

$\text{VCl}_4$  concentration of 0.01 mol/l, polymerization solution of 0.1 l.

TABLE 3. POLYMERIZATION RESULTS OBTAINED  
AT  $-78^{\circ}\text{C}$  WITH  $\text{VCl}_4/\text{AlEt}_3$   
CATALYST SYSTEM

Sample	$\text{AlEt}_3$ (mol/l)	$\text{C}_3\text{H}_6$ (mol/l)	Polymeri- zation period (h)	Poly- mer yield (g)	$\bar{M}_n$ ( $\times 10^5$ )	$Q$ ( $\bar{M}_w/\bar{M}_n$ )
C-1	0.025	8.4	0.5	0.30	2.57	1.6
C-2	0.025	8.4	1.0	0.49	3.43	1.8
C-3	0.025	8.4	1.5	0.92	5.45	2.0
C-4	0.025	8.4	2.5	1.25	7.55	2.0
C-5	0.025	8.4	3.0	1.43	7.75	2.0
C-6	0.005	8.4	3.0	1.08	6.81	2.1
C-7	0.015	8.4	3.0	0.83	5.97	2.4
C-8	0.100	8.4	3.0	0.57	4.86	2.6
C-9	0.150	8.4	3.0	0.40	3.46	2.6
C-10	0.200	8.4	3.0	0.47	3.82	2.2
C-11	0.025	1.2	2.5	0.22	2.74	2.1
C-12	0.025	4.8	2.5	0.82	5.74	2.0
C-13	0.025	11.9	2.5	1.42	10.7	1.8

$\text{VCl}_4$  concentration of 0.001 mol/l, polymerization solution of 0.1 l.

concentration,  $[\text{M}]$ .<sup>14)</sup>  $1/R_p$  is plotted against  $1/[\text{M}]$  for the respective catalyst system in Fig. 2. The linearity of the plots indicate that Eq. 5 is applicable to the polymerization of propene with soluble vanadium-based catalysts. The values of the coordination equilibrium constant of monomer,  $K_m$ , were determined from the slopes and the intercepts of the straight lines. The results are given in Table 4.

TABLE 4. RATE COEFFICIENTS OF ELEMENTARY REACTIONS IN THE POLYMERIZATION OF  
PROPENE WITH  $\text{VCl}_4/\text{AlEt}_2\text{X}$  ( $\text{X}=\text{Cl}, \text{Br}, \text{Et}$ ) CATALYST SYSTEMS AT  $-78^{\circ}\text{C}$

	$\text{AlEt}_2\text{Cl}$	$\text{AlEt}_2\text{Br}$	$\text{AlEt}_3$
$K_m(\text{l}\cdot\text{mol}^{-1})$	$0.26 \pm 0.03$	$0.02 \pm 0.01$	$0.04 \pm 0.01$
$K_A(\text{l}\cdot\text{mol}^{-1})$	$6.8 \pm 0.3$	$31 \pm 3$	$46 \pm 2$
$k_p(\text{h}^{-1})$	$(4.3 \pm 1.0) \times 10^3$	$(2.5 \pm 1.2) \times 10^2$	$(5.3 \pm 0.6) \times 10^4$
$k_{tm}(\text{h}^{-1})$	$5.4 \pm 0.1$	$1.7 \pm 0.1$	$2.3 \pm 0.3$
$k_{ta1}(\text{l}\cdot\text{mol}^{-1}\cdot\text{h}^{-1})$	$18 \pm 6.5$	$3.5 \pm 2.0$	$9.0 \pm 1.5$

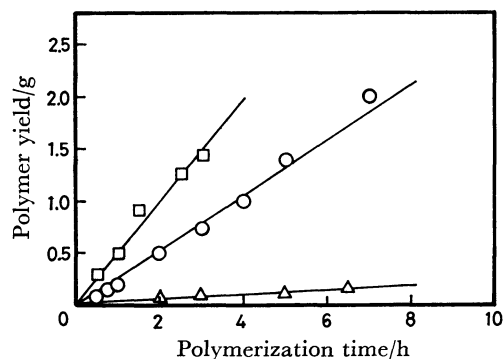


Fig. 1. Polymer yield-time curves of the polymerizations with different catalyst systems.

( $\circ$ );  $\text{VCl}_4/\text{AlEt}_2\text{Cl}$  system (samples A-1—A-8), ( $\triangle$ );  $\text{VCl}_4/\text{AlEt}_2\text{Br}$  system (samples B-1—B-4), ( $\square$ );  $\text{VCl}_4/\text{AlEt}_3$  system (samples C-1—C-5).

For experimental conditions see Tables 1—3.

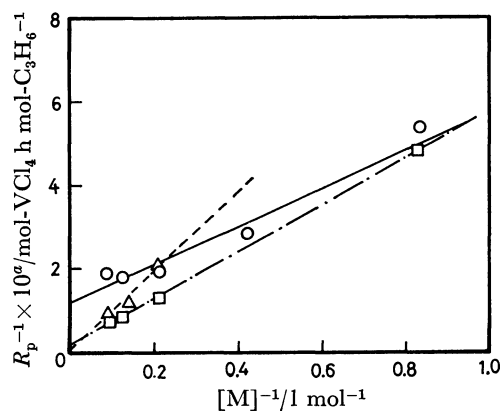


Fig. 2. Plots of the reciprocal of polymerization rate,  $R_p^{-1}$ , against the reciprocal of propene monomer concentration,  $[\text{M}]^{-1}$ .

( $\circ$ );  $\text{VCl}_4/\text{AlEt}_2\text{Cl}$  system ( $a=1$  for  $R_p^{-1} \times 10^a$ ), ( $\triangle$ );  $\text{VCl}_4/\text{AlEt}_2\text{Br}$  system ( $a=0$  for  $R_p^{-1} \times 10^a$ ), ( $\square$ );  $\text{VCl}_4/\text{AlEt}_3$  system ( $a=2$  for  $R_p^{-1} \times 10^a$ ).  
 $-78^{\circ}\text{C}$ ,  $[\text{AlEt}_2\text{Cl}] = [\text{AlEt}_2\text{Br}] = 0.05 \text{ mol/l}$  or  $[\text{AlEt}_3] = 0.025 \text{ mol/l}$ .

The effect of alkylaluminum concentration on the polymerization rate is complicated (Fig. 3). The polymerization rate rises to a maximum value followed by a gradual fall with increase in the concentration of alkylaluminum, *i.e.*, in the  $\text{Al}/\text{V}$  ratio. The polymerization rate is correlated with the following function of the concentration of alkylaluminum  $[\text{A}]$ .

$$R_p \propto \frac{K_A[\text{A}]}{(1 + K_A[\text{A}])^2} \quad (16)$$

The value of the constant,  $K_A$ , decreases in the order:  $\text{AlEt}_3 > \text{AlEt}_2\text{Br} > \text{AlEt}_2\text{Cl}$  (Table 4). The order appears to correspond to the reducing powers of the alkylaluminum for  $\text{VCl}_4$ . Though we can not present a conclusive explanation for Eq. 16, alkylaluminum seems to take part in the deactivation of polymerization centers as well as in the formation of the centers through the alkylation and complexation of  $\text{VCl}_4$ . This is supported by the observation of Lehr<sup>15</sup> that higher Al/V ratios result in some reduction of vanadium to its divalent state at  $-78^\circ\text{C}$  in the  $\text{VCl}_4/\text{Al}(i\text{-Bu})_3$  catalyst system. The influence of the alkylaluminum concentration on the polymerization rate is thus understandable as a result of the change in the number of polymerization centers,  $\sum_1 ([C_n] + [R_n])$ .

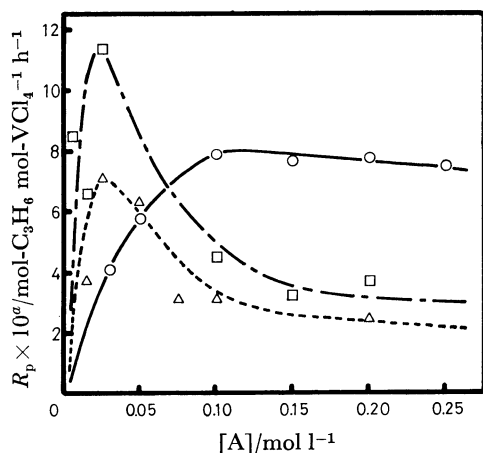


Fig. 3. Influence of alkylaluminum concentration,  $[A]$ , on polymerization rate,  $R_p$ . (O);  $\text{VCl}_4/\text{AlEt}_2\text{Cl}$  system ( $a=0$  for  $R_p \times 10^4$ ), ( $\Delta$ );  $\text{VCl}_4/\text{AlEt}_2\text{Br}$  system ( $a=-1$  for  $R_p \times 10^4$ ), ( $\square$ );  $\text{VCl}_4/\text{AlEt}_3$  system ( $a=1$  for  $R_p \times 10^4$ ).  $-78^\circ\text{C}$ ,  $[M]=8.4 \text{ mol/l}$ .

**Average Molecular Weight.** The number-average molecular weights,  $\bar{M}_n$ , of polymers produced increase with the polymerization time, attaining constant values in a few hours for all the catalyst systems (Tables 1–3). The plots of  $1/\bar{M}_n$  vs.  $1/t$  are shown for different catalyst systems in Fig. 4. The linearity of plots indicates that the experimental results are satisfactorily correlated by Eq. 8, which is a linear form of Eq. 7. Using the values of  $K_m$  given in the preceding section, we can estimate the values of the propagation rate coefficient of monomer,  $k_p$ , from the slopes of the straight lines. The values of  $k_p$  for different catalyst systems are summarized in Table 4.

The values of  $\bar{M}_n$  of the polymers produced at 3 h increase with increase in the concentration of propene monomer,  $[M]$ . The dependence of the value of  $\bar{M}_n$  on  $[M]$  is given by Eq. 9. The relation between the value of  $\bar{M}_n$  of the polymers produced and the concentration of alkylaluminums,  $[A]$ , also follows Eq. 9 (Figs. 5–7). The values of intercepts of both straight lines in the respective figure agree closely with each other. This suggests that the chain terminating steps other than the transfer with monomer and alkylalumi-

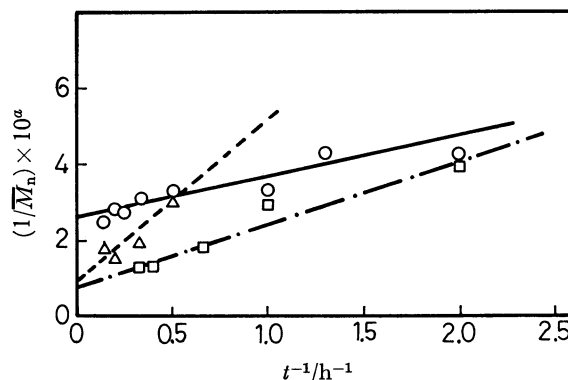


Fig. 4. Plots of  $1/\bar{M}_n$  vs.  $1/t$ . (O);  $\text{VCl}_4/\text{AlEt}_2\text{Cl}$  system ( $a=5$  for  $1/\bar{M}_n \times 10^4$ , samples A-1–A-8), ( $\Delta$ );  $\text{VCl}_4/\text{AlEt}_2\text{Br}$  system ( $a=4$  for  $1/\bar{M}_n \times 10^4$ , samples B-1–B-4), ( $\square$ );  $\text{VCl}_4/\text{AlEt}_3$  system ( $a=6$  for  $1/\bar{M}_n \times 10^4$ , samples C-1–C-5). For experimental conditions see Table 1–3.

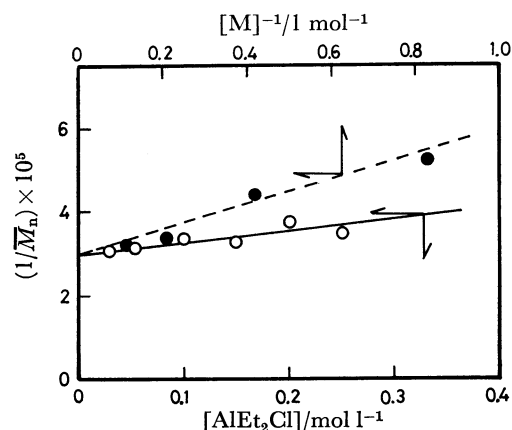


Fig. 5. Plots of  $1/\bar{M}_n$  vs.  $1/[M]$  and vs.  $[A]$  for  $\text{VCl}_4/\text{AlEt}_2\text{Cl}$  system. (●); Samples A-14–A-16 and A-5, (○); Samples A-9–A-13 and A-5. For experimental conditions see Table 1.

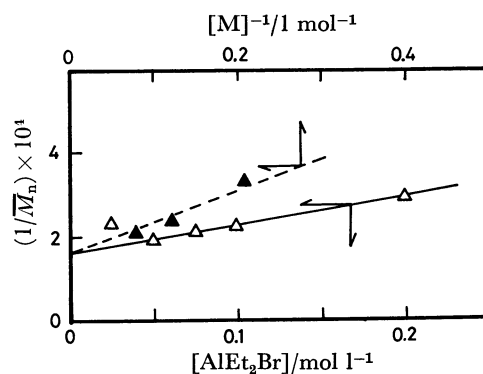


Fig. 6. Plots of  $1/\bar{M}_n$  vs.  $1/[M]$  and vs.  $[A]$  for  $\text{VCl}_4/\text{AlEt}_2\text{Br}$  system. (▲); Samples B-10, B-11 and B-2, ( $\Delta$ ); Samples B-6–B-9 and B-2. For experimental conditions see Table 2.

nium is not significant in the polymerization. The values of the rate coefficients of the chain transfers,  $k_{tm}$  and

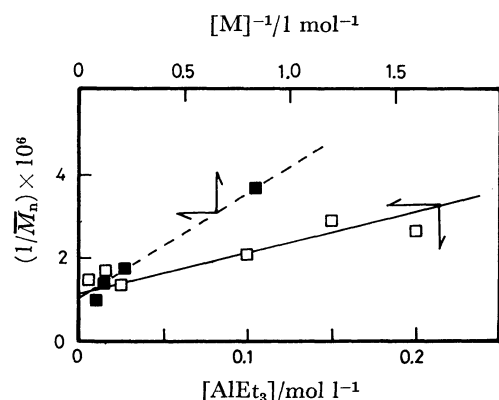


Fig. 7. Plots of  $1/\bar{M}_n$  vs.  $1/[M]$  and vs.  $[A]$  for  $VCl_4/AlEt_3$  system.

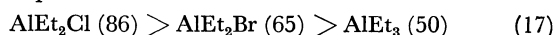
(■); Samples C-11—C-13 and C-4.

(□); Samples C-5—C-10.

For experimental conditions see Table 3.

$k_{tal}$ , may be obtained from the intercepts and slopes of the straight lines. The values of  $k_{tm}$  and  $k_{tal}$  are given in Table 4 with the experimental deviation for each catalyst system.

The rate coefficients of the elementary reactions are remarkably affected by the type of alkylaluminum used. The mole fraction of syndiotactic dyads of the polypropylene produced decreases as follows.<sup>7)</sup>



The remarkable influence of the type of alkylaluminum on the elementary reaction rates and stereospecificity may be interpreted in terms of the bimetallic structure of the polymerization center, first proposed by Zambelli *et al.*,<sup>11)</sup> in which the alkylaluminum complexed with alkylvanadium chloride regulates the catalytic capability.

**Molecular Weight Distributions.** Comparison has been made between the theoretical and experimental MWD curves of the polypropylene samples. Three

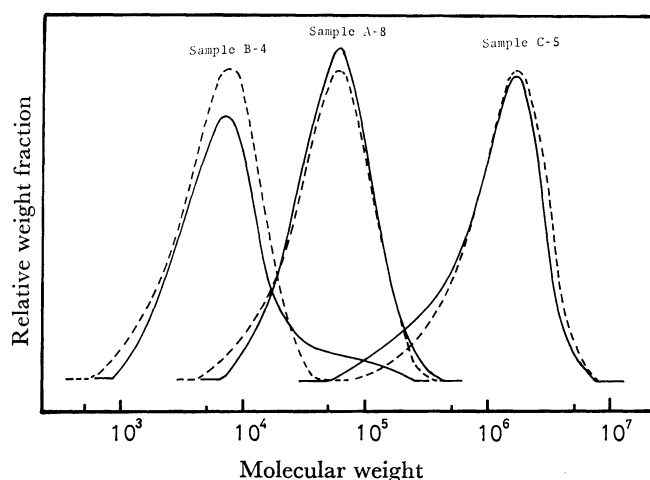


Fig. 8. Experimental and theoretical molecular weight distribution curves of polypropylenes prepared at  $-78^\circ C$  with different soluble vanadium-based catalysts.

(—): Experimental curves, (---) theoretical curves.

normalized GPC curves of samples A-8, B-4 and C-5 are shown in Fig. 8 by solid lines. The polypropylene samples were prepared by the polymerization with different catalyst systems. The weight fraction of polymer is plotted against common logarithms of molecular weight. For the sake of comparison the theoretical MWD curves of the three samples were calculated from a plot of  $42 \cdot n^2 \cdot [X(n)]$  vs.  $\log (42 \cdot n)$ , with  $[X(n)]$  by means of Eq. 15 and the values of  $\beta$  (0.99865 for sample A-8, 0.98915 for sample B-4 and 0.99995 for sample C-5) were determined using the kinetic parameters (Table 4), taking the conditions for the preparation into consideration. The results are shown in Fig. 8 by dotted lines. The modes of curves and the values of maxima are in close agreement between theory and experiment, except sample B-4 prepared with  $VCl_4/AlEt_2Br$  system. The shoulder at the higher molecular weights observed in the GPC curve of sample B-4 may be due to the coexistence of  $AlEt_2Cl$  formed by the halogen interchange between  $VCl_4$  and  $AlEt_2Br$ .

It may be concluded that the molecular weight distributions of polymers produced with soluble vanadium-based catalysts are expressed by the distribution function of Eq. 15 derived from the kinetic scheme proposed.

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